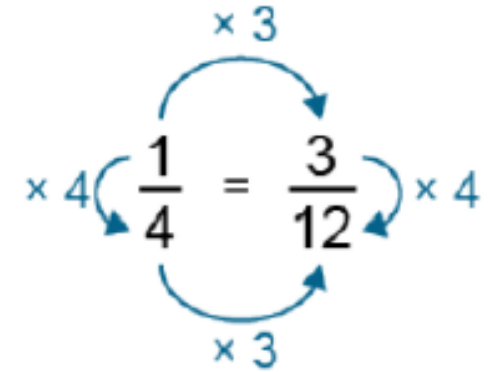
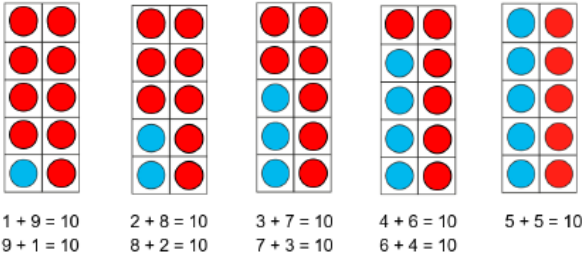


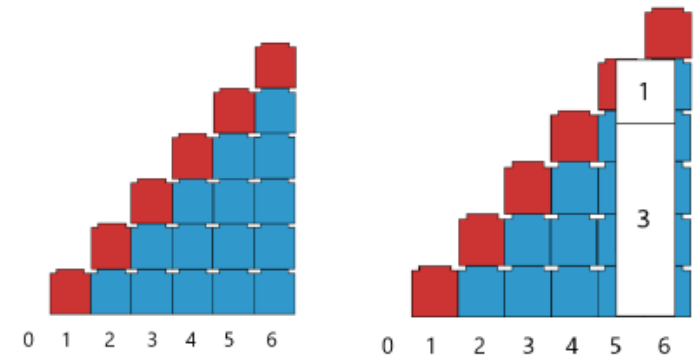
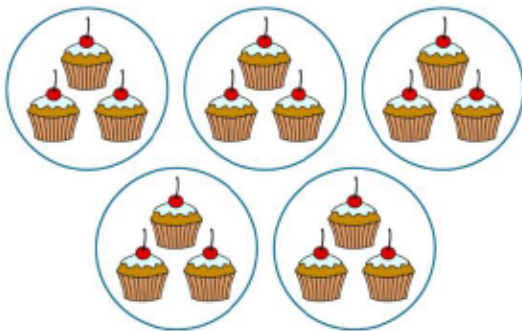


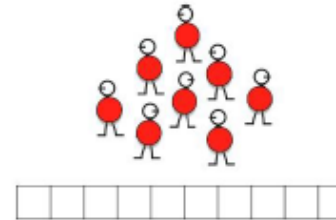
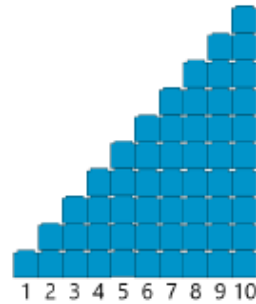
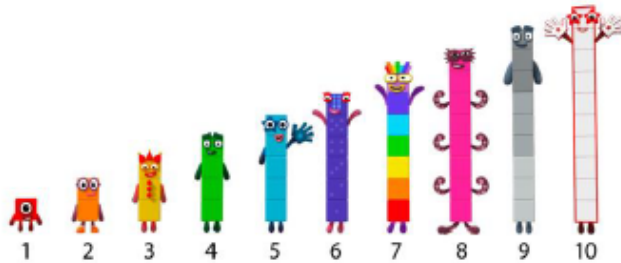
Visual Coding

Key Representations

Progression from years 1-6

Autumn Term





1	2	3	4	5	6	7	8	9	10
one	two	three	four	five	six	seven	eight	nine	ten

A



B



Adam



Nick



Tom



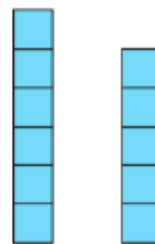
$$1 < 3$$



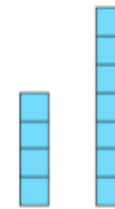
$$2 = 2$$



$$3 > 1$$



$$6 > 5$$

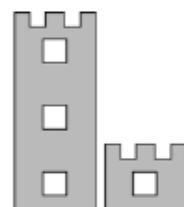
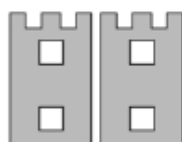
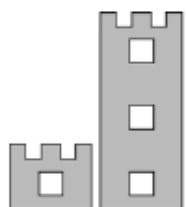
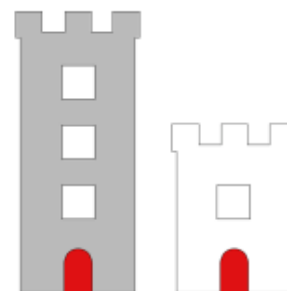


$$4 < 7$$



$$6 = 6$$

Year 1:1.2



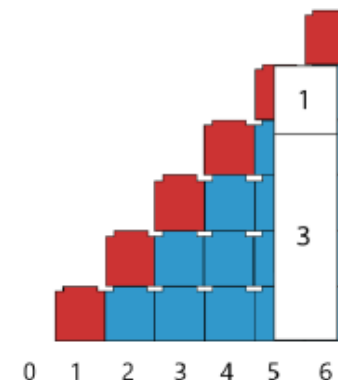
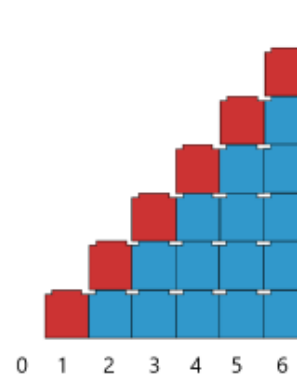
$$1 < 3$$



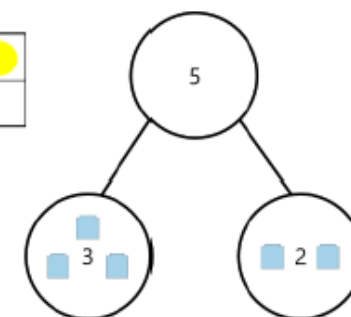
$$2 = 2$$



$$3 > 1$$



6

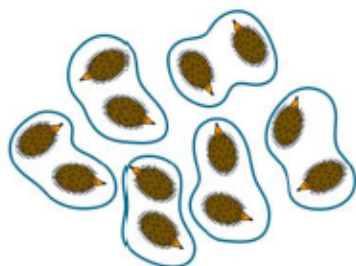


How many shoes are there?

Count in groups of two.



How many hedgehogs are there?



zero
0

two
2

four
4

six
6

eight
8

ten
10

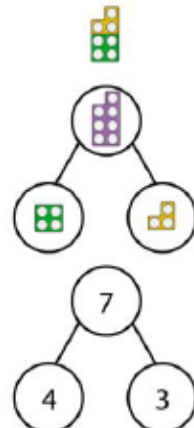
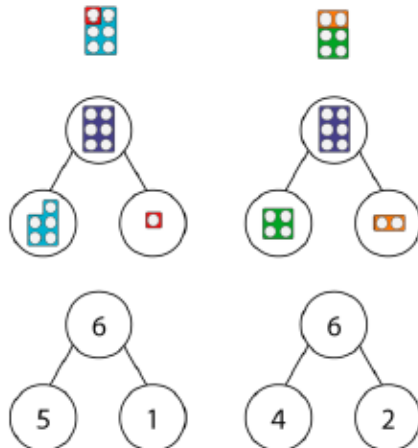
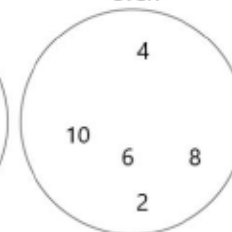
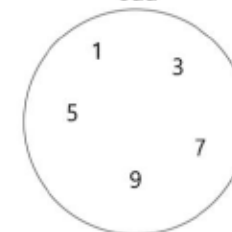
odd

even



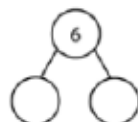
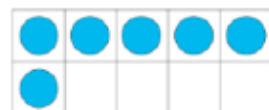
odd

even

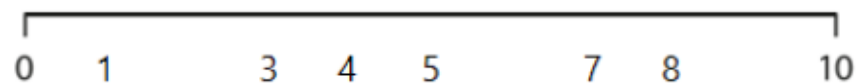




6



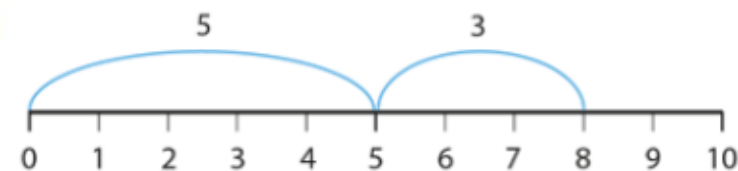
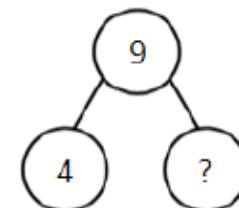
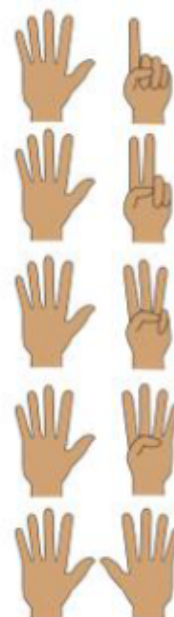
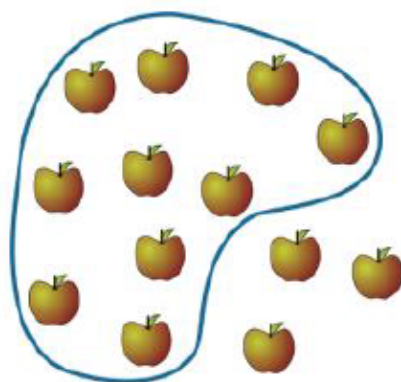
6				
5				1



2

9

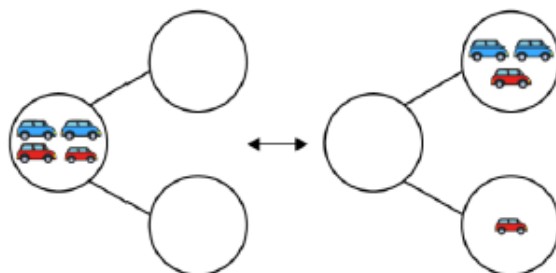
6



10s	1s

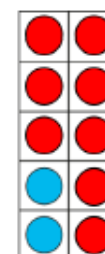
Year 2: 2.1

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



$$1 + 9 = 10$$

$$9 + 1 = 10$$



$$2 + 8 = 10$$

$$8 + 2 = 10$$



$$3 + 7 = 10$$

$$7 + 3 = 10$$

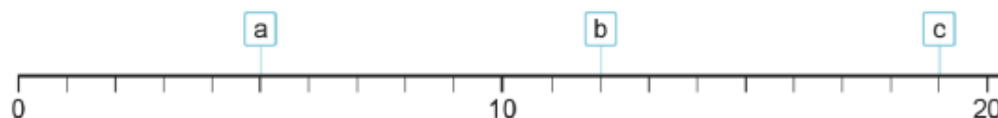
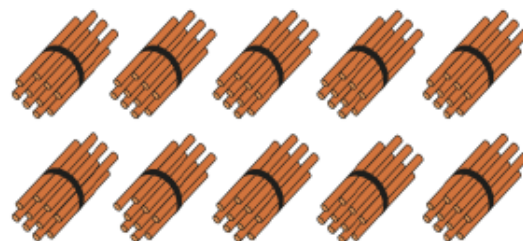


$$4 + 6 = 10$$

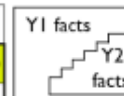
$$6 + 4 = 10$$



$$5 + 5 = 10$$



+	0	1	2	3	4	5	6	7	8	9	10
0	0+0	0+1	0+2	0+3	0+4	0+5	0+6	0+7	0+8	0+9	0+10
1	1+0	1+1	1+2	1+3	1+4	1+5	1+6	1+7	1+8	1+9	1+10
2	2+0	2+1	2+2	2+3	2+4	2+5	2+6	2+7	2+8	2+9	2+10
3	3+0	3+1	3+2	3+3	3+4	3+5	3+6	3+7	3+8	3+9	3+10
4	4+0	4+1	4+2	4+3	4+4	4+5	4+6	4+7	4+8	4+9	4+10
5	5+0	5+1	5+2	5+3	5+4	5+5	5+6	5+7	5+8	5+9	5+10
6	6+0	6+1	6+2	6+3	6+4	6+5	6+6	6+7	6+8	6+9	6+10
7	7+0	7+1	7+2	7+3	7+4	7+5	7+6	7+7	7+8	7+9	7+10
8	8+0	8+1	8+2	8+3	8+4	8+5	8+6	8+7	8+8	8+9	8+10
9	9+0	9+1	9+2	9+3	9+4	9+5	9+6	9+7	9+8	9+9	9+10
10	10+0	10+1	10+2	10+3	10+4	10+5	10+6	10+7	10+8	10+9	10+10



Adding 1

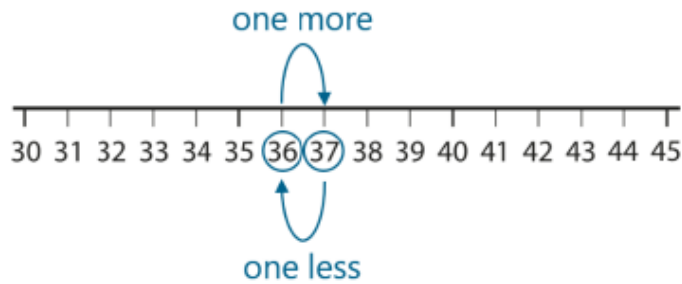
Adding 2

Bonds to 10

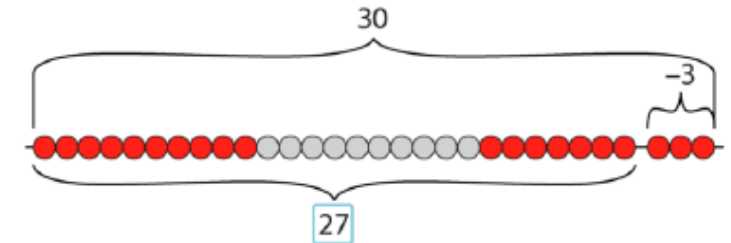
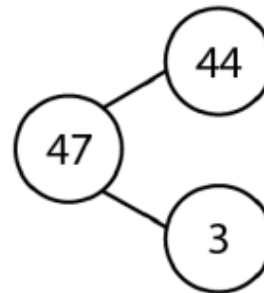
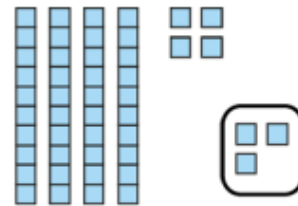
Adding 0

Doubles

Near doubles



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

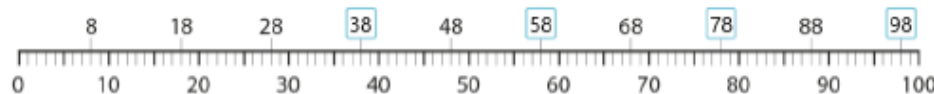
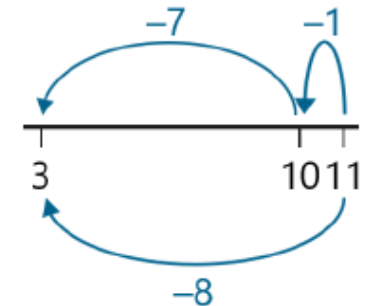
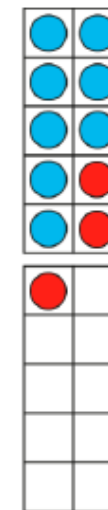
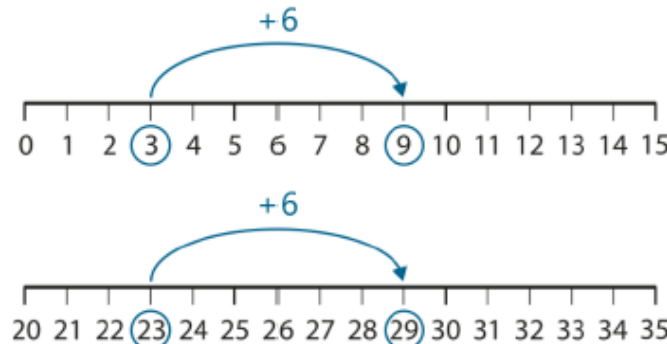


$$8 + 3 = 11$$

2 1

$$11 - 8 = 3$$

1 7



Year 2: 2.3

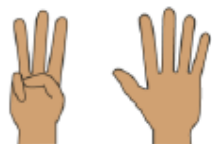


Figure 17: 8 represented as 3 fingers and 5 fingers



Figure 18: 8 represented as 6 and 2 with base 10 number boards

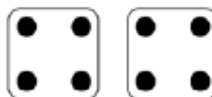


Figure 19: 8 represented as two 4-value dice



Figure 20: 8 represented as 2 rows of 4



Figure 21: 8 represented as tally marks: 5 and 3



Figure 22: 8 represented on a bead string: 7 and 1



$$5 + 2 = 7$$



Figure 30: aggregation or partitioning context: 5 cakes altogether, 2 with cherries and 3 without

$$2 + 3 = 5$$

$$5 - 3 = 2$$

$$5 = 2 + 3$$

$$2 = 5 - 3$$

$$3 + 2 = 5$$

$$5 - 2 = 3$$

$$5 = 3 + 2$$

$$3 = 5 - 2$$

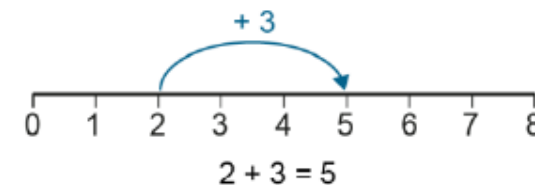
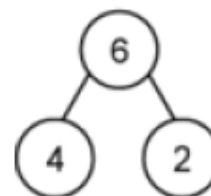


7	
5	2

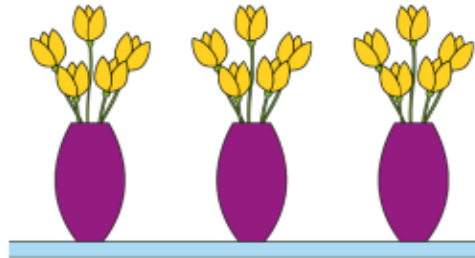
$$7 - 2 = 5$$



$$3 + 1 = 4$$

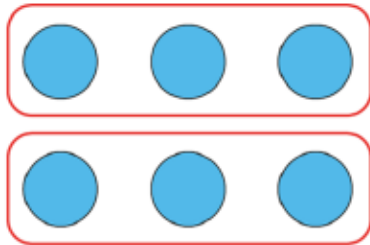


Year 2: 2.4



$$5 + 5 + 5$$

$$3 \times 5$$

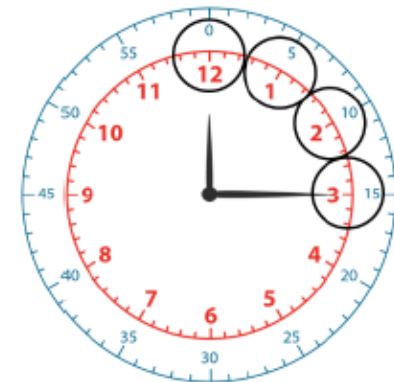
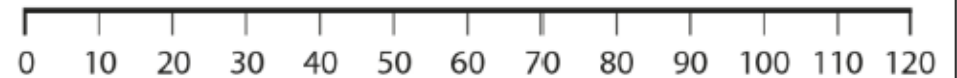
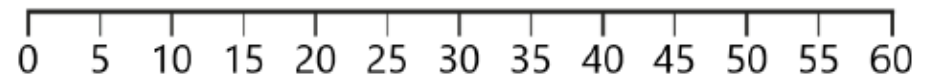
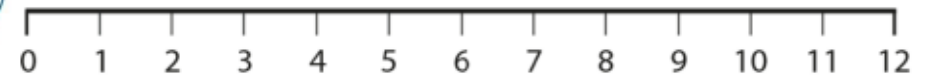


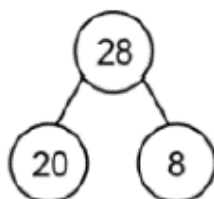
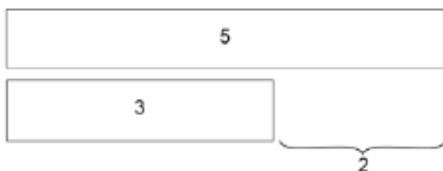
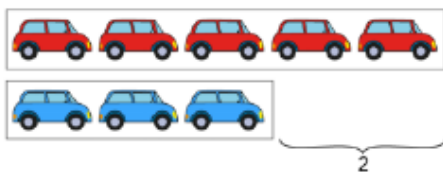
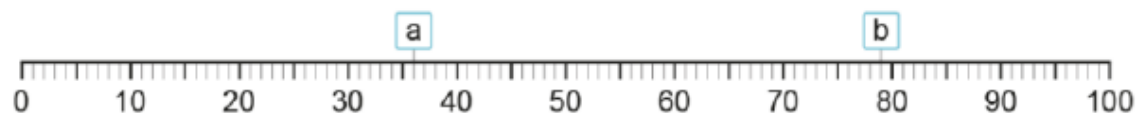
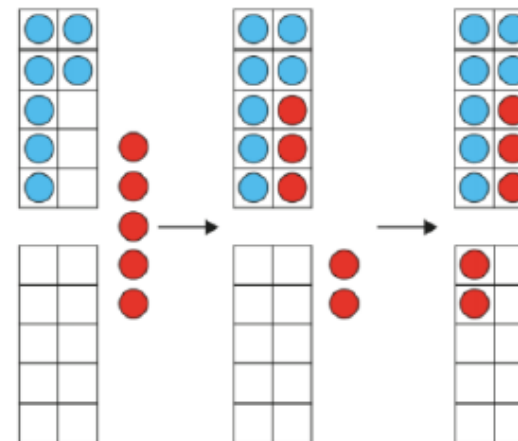
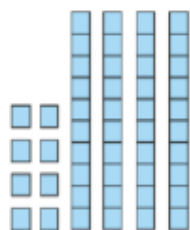
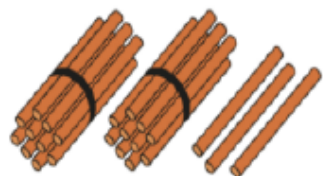
$$2 \times 3$$

This represents $3 + 3$.



1000	2000	3000	4000	5000	6000	7000	8000	9000
100	200	300	400	500	600	700	800	900
10	20	30	40	50	60	70	80	90
1	2	3	4	5	6	7	8	9





28	
20	8

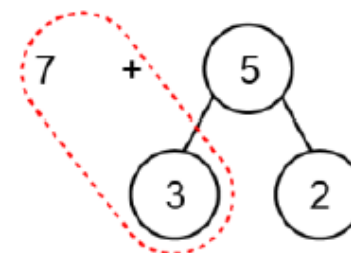
$$20 + 8 = 28 \quad 28 - 20 = 8$$

$$8 + 20 = 28 \quad 28 - 8 = 20$$

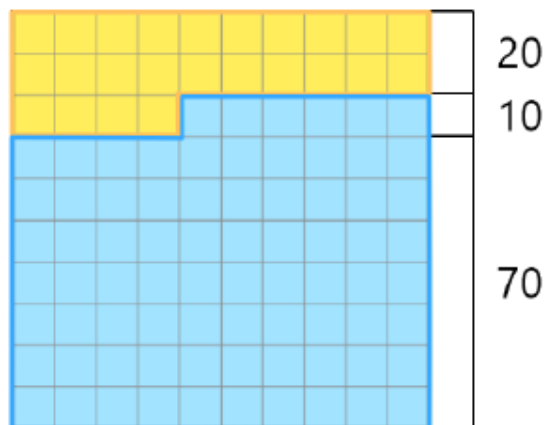
$$28 = 20 + 8 \quad 8 = 28 - 20$$

$$28 = 8 + 20 \quad 20 = 28 - 8$$

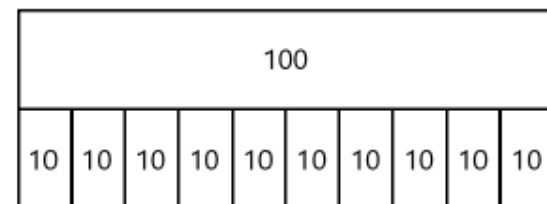
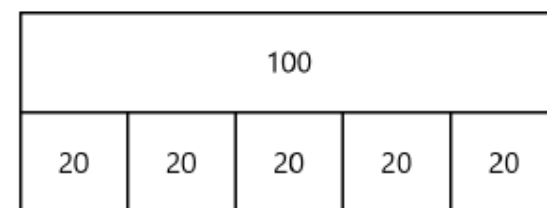
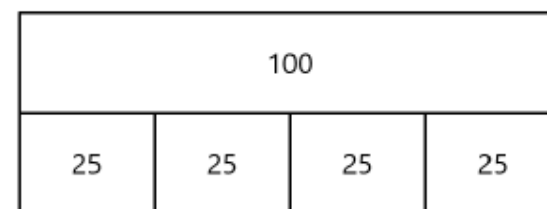
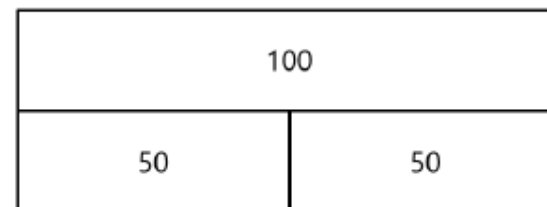
$$7 + 5 = 12$$



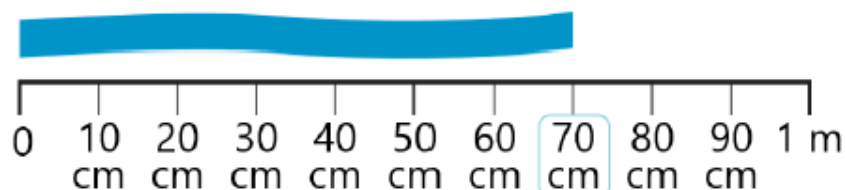
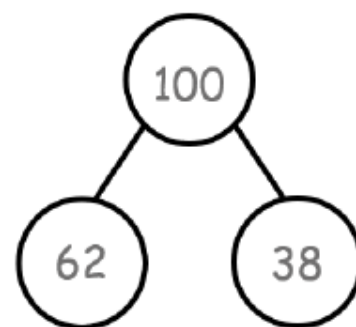
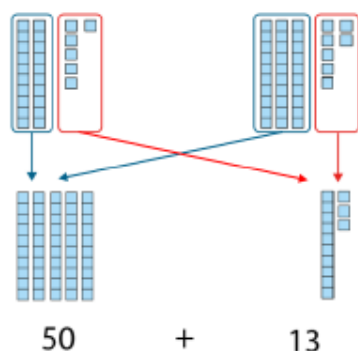
$$24 + 76 = 100$$



$$\begin{array}{r} 24 + 76 = 100 \\ \swarrow \searrow \quad \swarrow \searrow \\ 20 \quad 4 \quad 6 \quad 70 \\ \quad \quad \quad 10 \end{array}$$



$$26 + 37 = 63$$



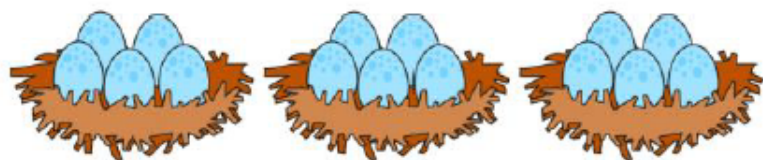


Figure 52: recognising equal groups – 3 groups of 5 eggs

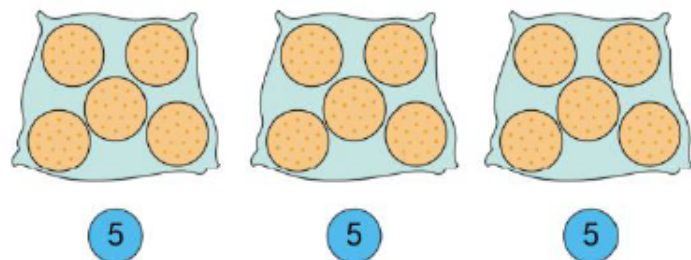
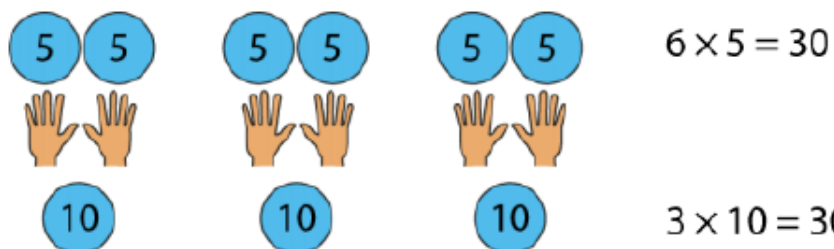


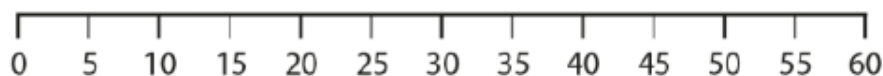
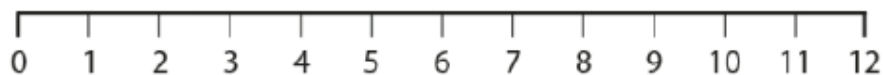
Figure 54: 3 bags of 5 biscuits alongside three 5-value counters



$$6 \times 5 = 30$$

$$3 \times 10 = 30$$

Stacked number lines:

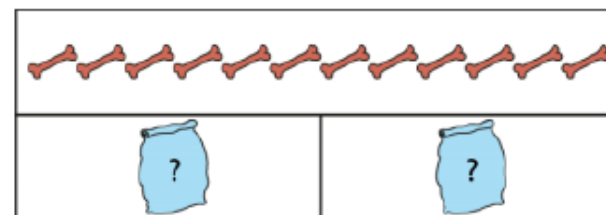


8	
4	4

$$2 \times 4 = 8$$

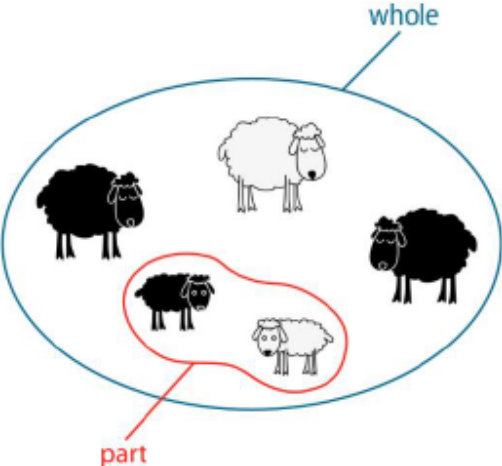
Half of 8 is equal to ____.
Double ____ is equal to 8.

$6 \times 2 = 12$	
<i>'Six times two can represent six groups of two.'</i>	<i>'It can also represent two groups of six (or six, two times).'</i>

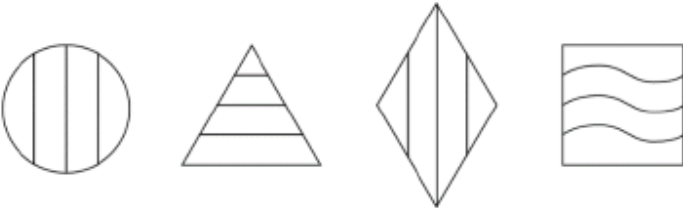


$$2 \times \square = 12$$

$$\square \times 2 = 12$$



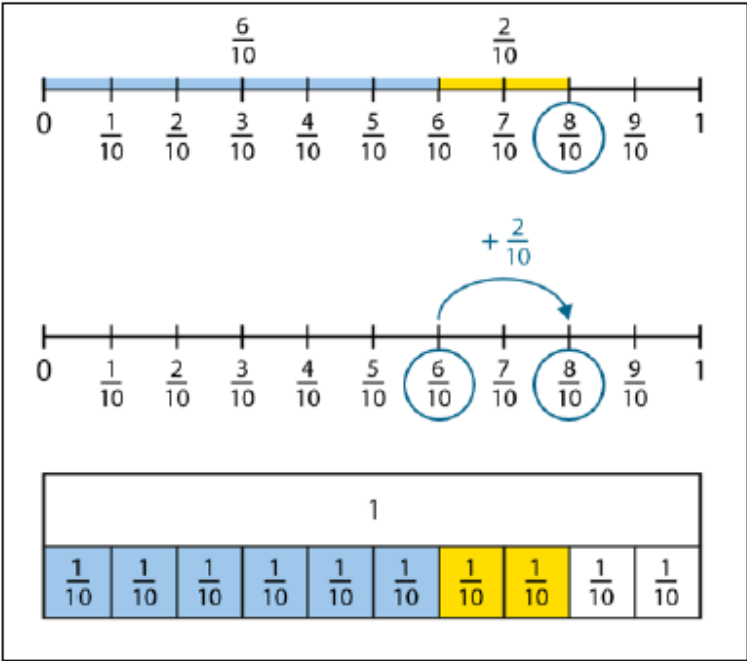
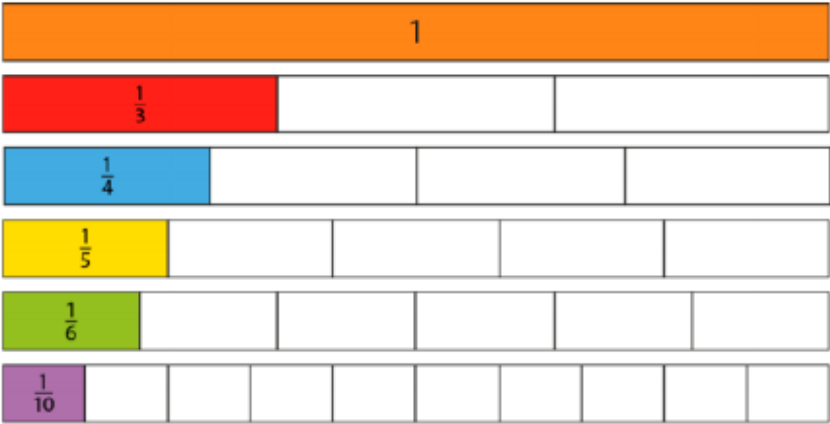
Equal or unequal parts?



4 equal parts

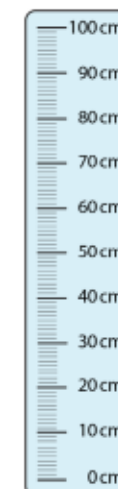
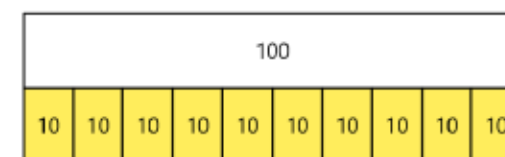
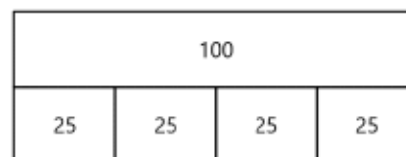
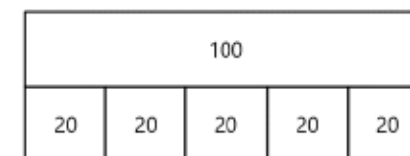
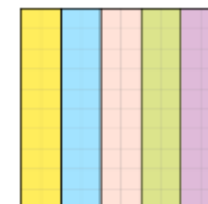
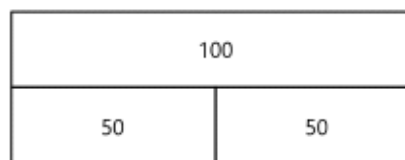
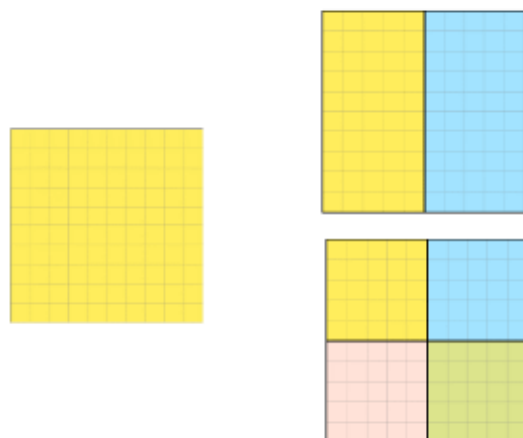


4 unequal parts

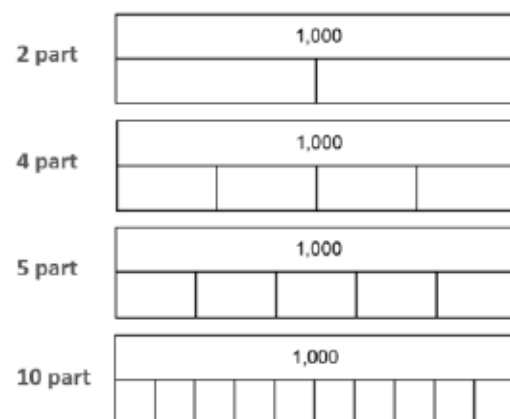


Year 3: 3.5

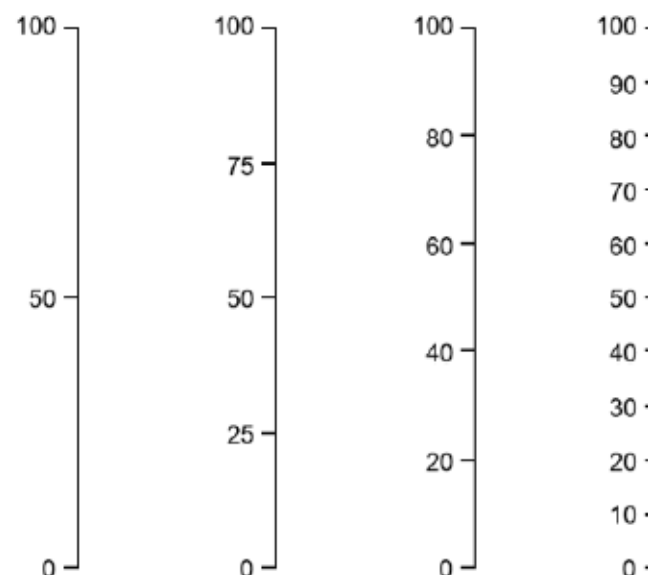
2, 4, 5 and 10 part composition of 100

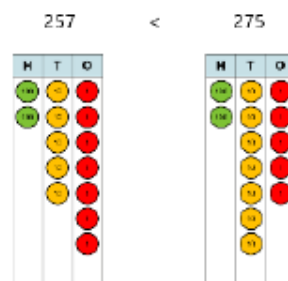
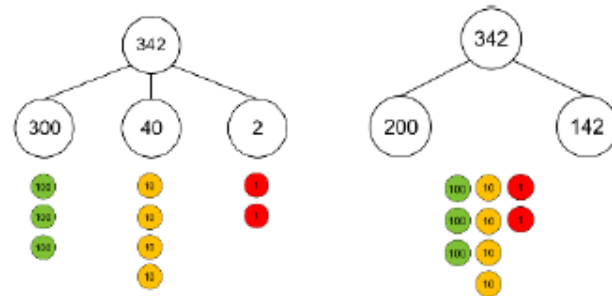


2, 4, 5 and 10 part composition of 1,000



Related to scale





342

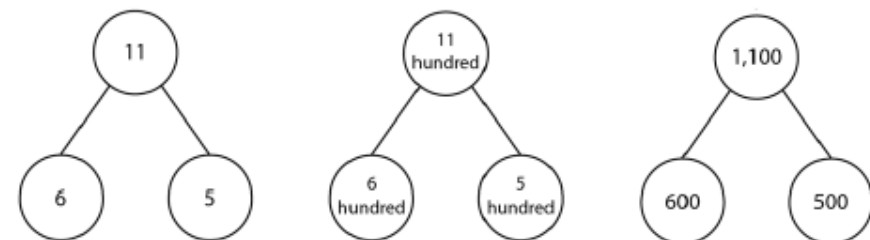
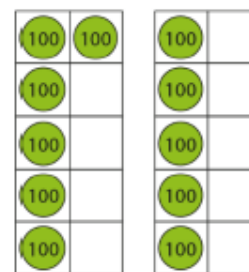
1,000	2,000	3,000	4,000	5,000	6,000	7,000	8,000	9,000
100	200	300	400	500	600	700	800	900
10	20	30	40	50	60	70	80	90
1	2	3	4	5	6	7	8	9

$$300 + 40 + 2 = 342$$

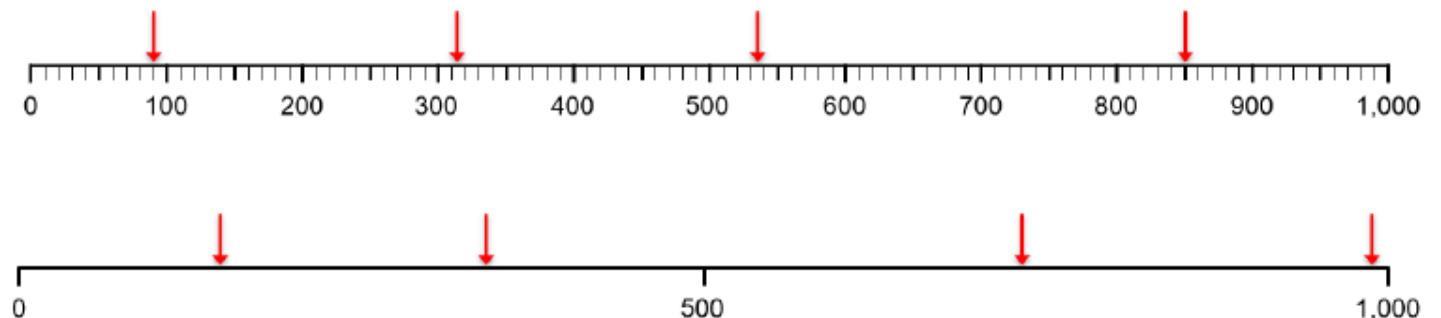
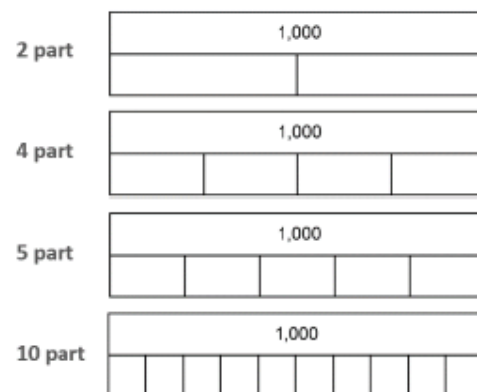
1,400

$$600 + 500 = 1,100$$

1,000s	100s	10s	1s
1	4	0	0



2, 4, 5 and 10 part composition of 1,000



Part Part Whole
↓ ↓ ↓
 $329 + \boxed{414} = 743$

743	
329	414

$743 - 329 = \boxed{414}$

Whole Part Part
↓ ↓ ↓
 $\boxed{614} - 527 = 87$

614	
527	87

$527 + 87 = \boxed{614}$

Whole Part Part
↓ ↓ ↓
 $\boxed{614} - 527 = 87$

614	
527	87

$527 + 87 = \boxed{614}$

+	0	1	2	3	4	5	6	7	8	9	10
0	0+0	0+1	0+2	0+3	0+4	0+5	0+6	0+7	0+8	0+9	0+10
1	1+0	1+1	1+2	1+3	1+4	1+5	1+6	1+7	1+8	1+9	1+10
2	2+0	2+1	2+2	2+3	2+4	2+5	2+6	2+7	2+8	2+9	2+10
3	3+0	3+1	3+2	3+3	3+4	3+5	3+6	3+7	3+8	3+9	3+10
4	4+0	4+1	4+2	4+3	4+4	4+5	4+6	4+7	4+8	4+9	4+10
5	5+0	5+1	5+2	5+3	5+4	5+5	5+6	5+7	5+8	5+9	5+10
6	6+0	6+1	6+2	6+3	6+4	6+5	6+6	6+7	6+8	6+9	6+10
7	7+0	7+1	7+2	7+3	7+4	7+5	7+6	7+7	7+8	7+9	7+10
8	8+0	8+1	8+2	8+3	8+4	8+5	8+6	8+7	8+8	8+9	8+10
9	9+0	9+1	9+2	9+3	9+4	9+5	9+6	9+7	9+8	9+9	9+10
10	10+0	10+1	10+2	10+3	10+4	10+5	10+6	10+7	10+8	10+9	10+10

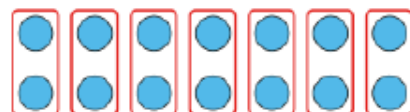


$8 + 6$

8 tens + 6 tens

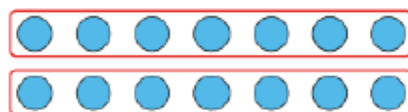
80 + 60

1,000	2,000	3,000	4,000	5,000	6,000	7,000	8,000	9,000
100	200	300	400	500	600	700	800	900
10	20	30	40	50	60	70	80	90
1	2	3	4	5	6	7	8	9



7 groups of 2

$$7 \times 2 = 14$$



2 groups of 7

$$2 \times 7 = 14$$

$$7 \times 2 = 2 \times 7$$

$0 \times 6 = 0$	$6 \times 0 = 0$
$1 \times 6 = 6$	$6 \times 1 = 6$
$2 \times 6 = 12$	$6 \times 2 = 12$
$3 \times 6 = 18$	$6 \times 3 = 18$
$4 \times 6 = 24$	$6 \times 4 = 24$
$5 \times 6 = 30$	$6 \times 5 = 30$
$6 \times 6 = 36$	$6 \times 6 = 36$
$7 \times 6 = 42$	$6 \times 7 = 42$
$8 \times 6 = 48$	$6 \times 8 = 48$
$9 \times 6 = 54$	$6 \times 9 = 54$
$10 \times 6 = 60$	$6 \times 10 = 60$
$11 \times 6 = 66$	$6 \times 11 = 66$
$12 \times 6 = 72$	$6 \times 12 = 72$

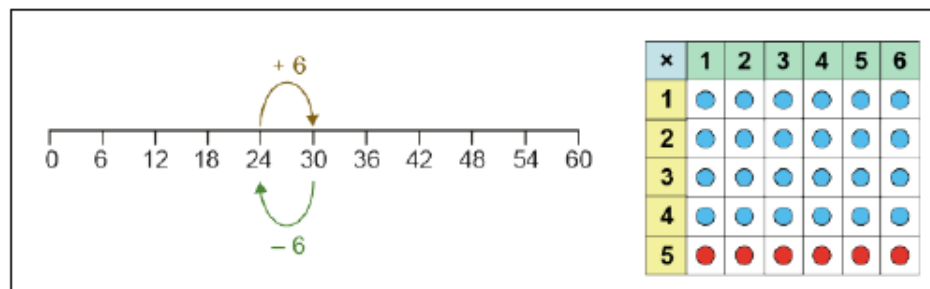
	$\times 7$
0	0
1	7
2	14
3	21
4	28
5	35
6	42
7	49
8	56
9	63
10	70
11	77
12	84

↓ + 7

↑ - 7

↓ + 7

↓ + 7



$14 \div 7 = 2$

Partitive division

Figure 121: 7 groups of 2 – 7 nests of 2 eggs and seven 2-value counters

Quotitive division

Figure 122: 2 groups of 7 – 2 nests of 7 eggs and two 7-value counters

Language focus

"14 shared between 7 is equal to 2."

"The 14 represents the total number of eggs."

"The 7 represents the number of nests/shares."

"The 2 represents the number of eggs in each nest/share."

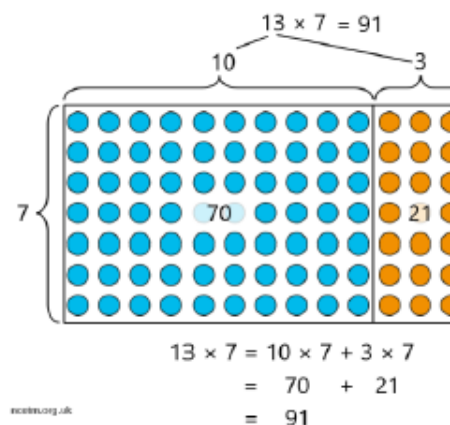
Language focus

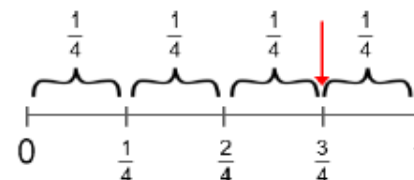
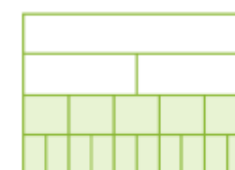
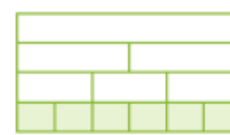
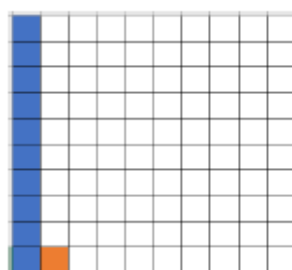
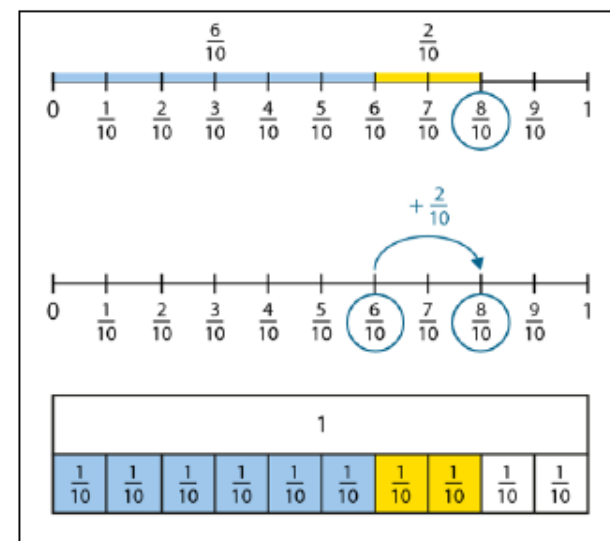
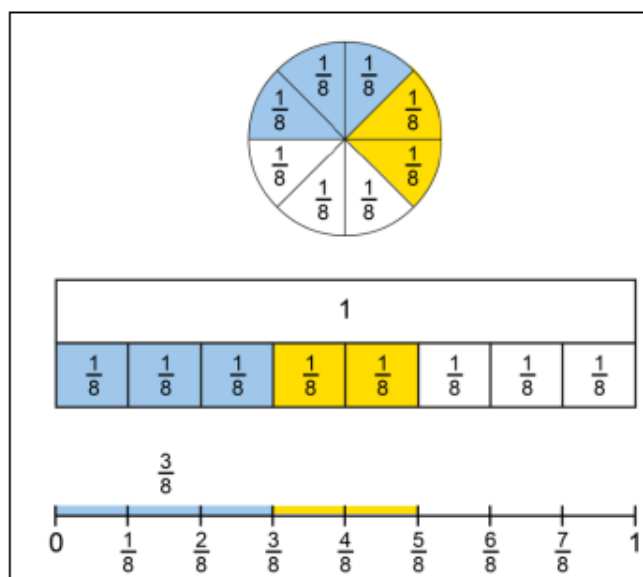
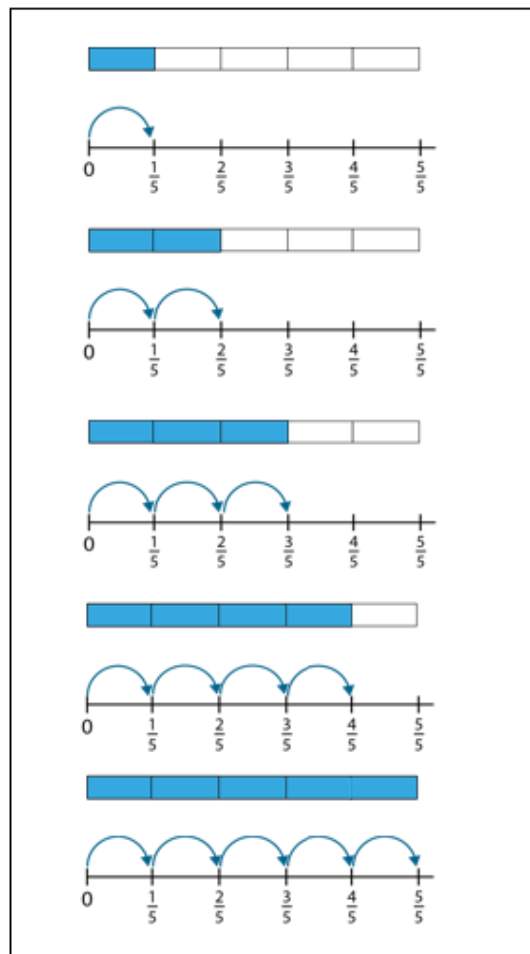
"14 divided into groups of 7 is equal to 2."

"The 14 represents the total number of eggs."

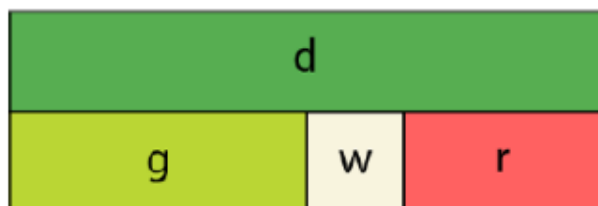
"The 7 represents the number of eggs in each nest/group."

"The 2 represents the number of nests/groups."





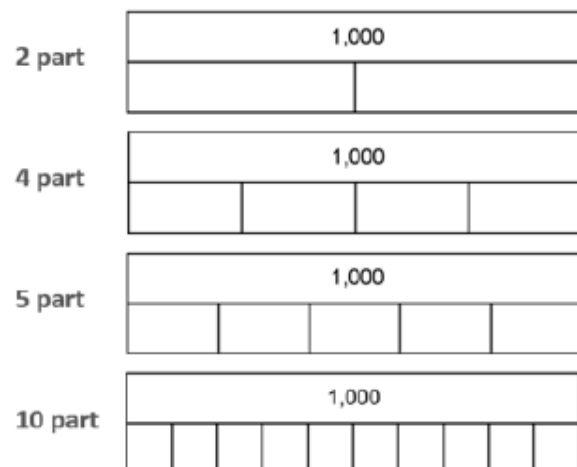
1. Additive – combining or partitioning



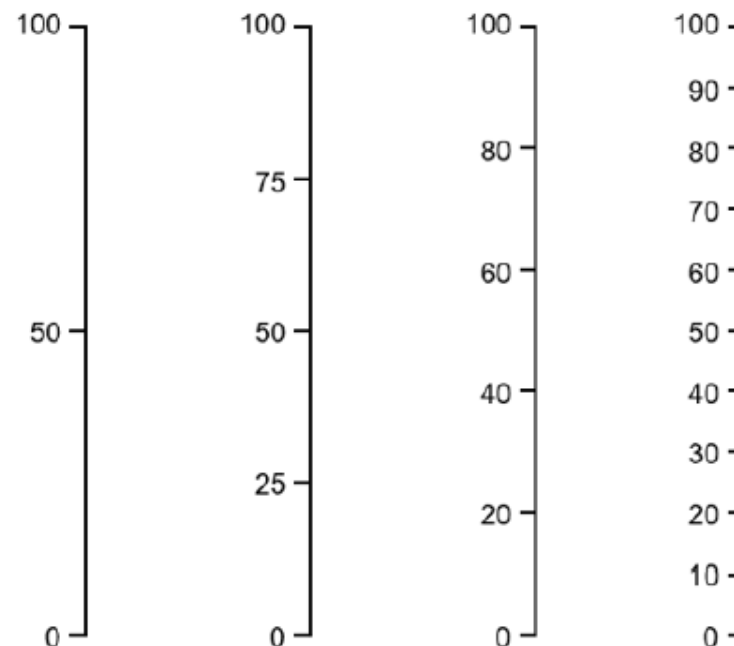
2. Additive – comparative

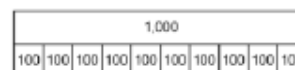
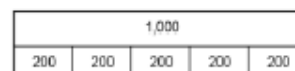
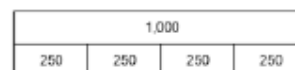
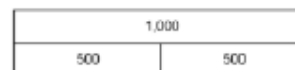
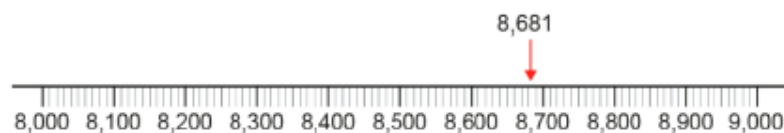
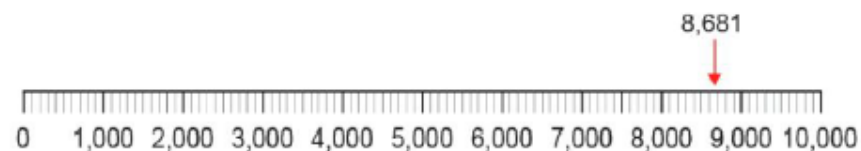
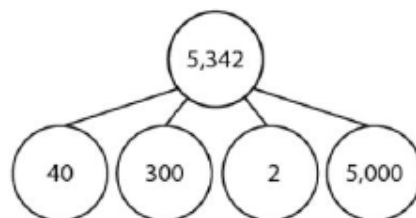
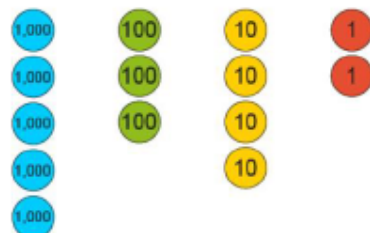
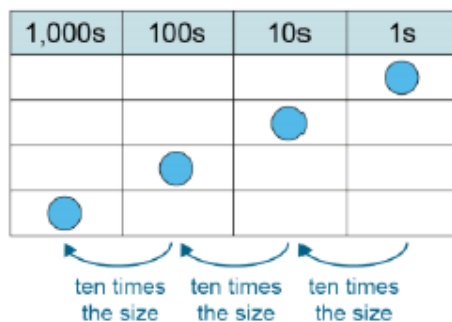


2, 4, 5 and 10 part composition of 1,000



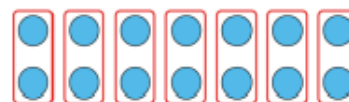
Related to scale



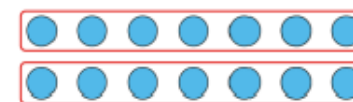


Year 5: 5.2

×	1	2	3	4	5	6
1	•	•	•	•	•	•
2	•	•	•	•	•	•
3	•	•	•	•	•	•
4	•	•	•	•	•	•
5	•	•	•	•	•	•



7 groups of 2
 $7 \times 2 = 14$



2 groups of 7
 $2 \times 7 = 14$

$$7 \times 2 = 2 \times 7$$

1,000	2,000	3,000	4,000	5,000	6,000	7,000	8,000	9,000
100	200	300	400	500	600	700	800	900
10	20	30	40	50	60	70	80	90
1	2	3	4	5	6	7	8	9

$$80 \times 10 = 800$$

$$80 \div 10 = 8$$

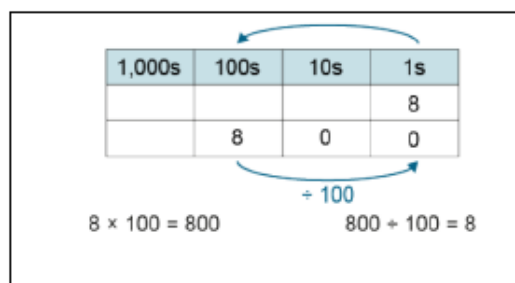
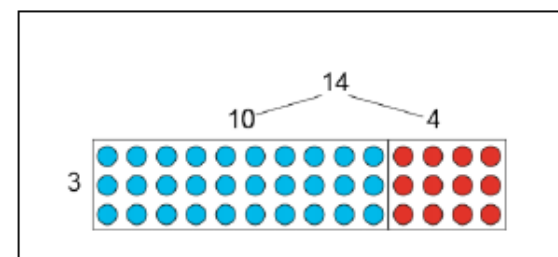


Figure 121: 7 groups of 2 – 7 nests of 2 eggs and seven 2-value counters

Language focus

"14 shared between 7 is equal to 2."

"The 14 represents the total number of eggs."

"The 7 represents the number of nests/shares."

"The 2 represents the number of eggs in each nest/share."



Figure 122: 2 groups of 7 – 2 nests of 7 eggs and two 7-value counters

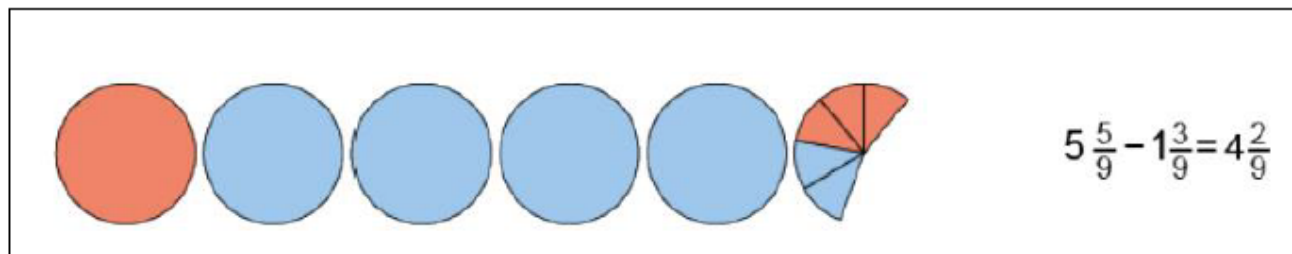
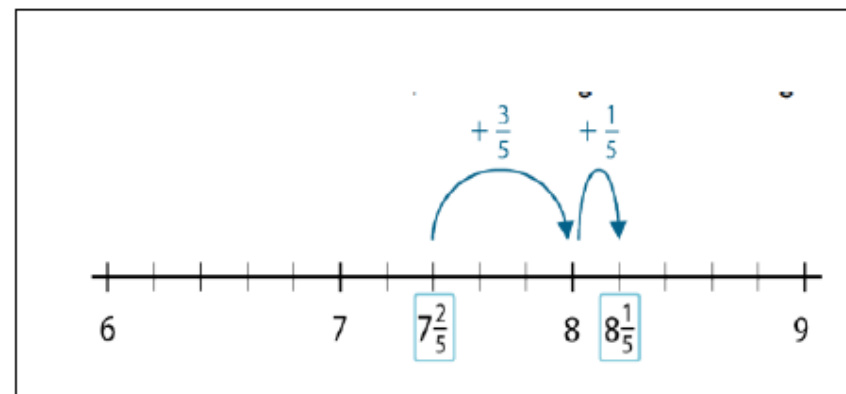
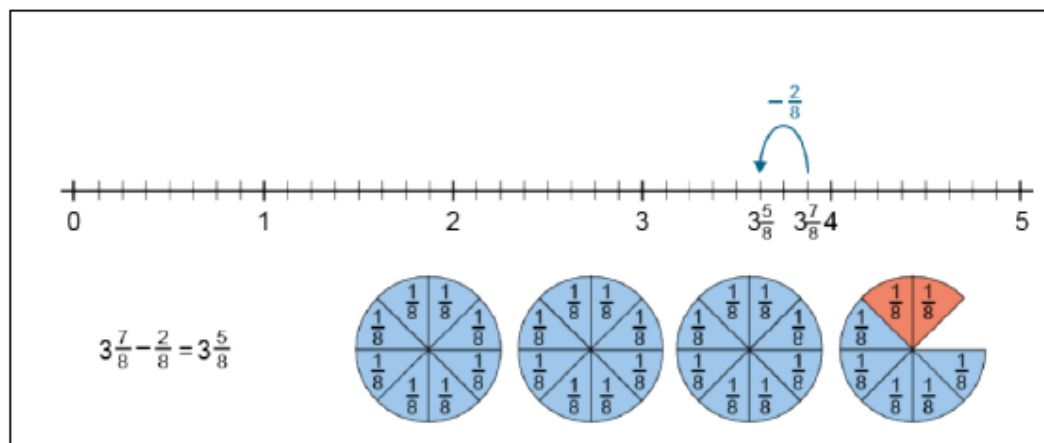
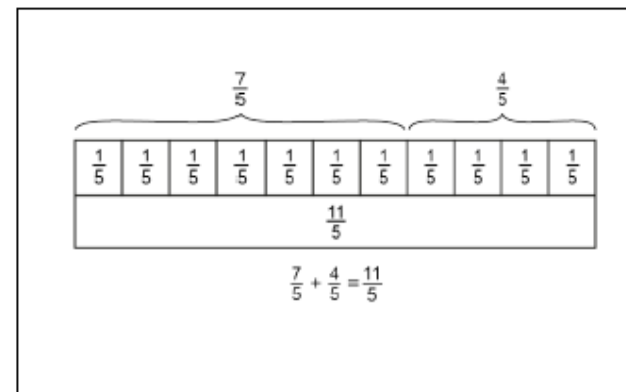
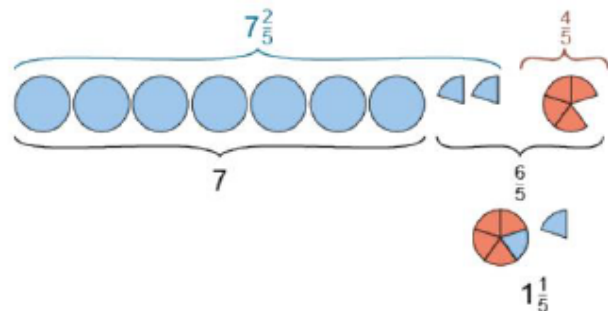
Language focus

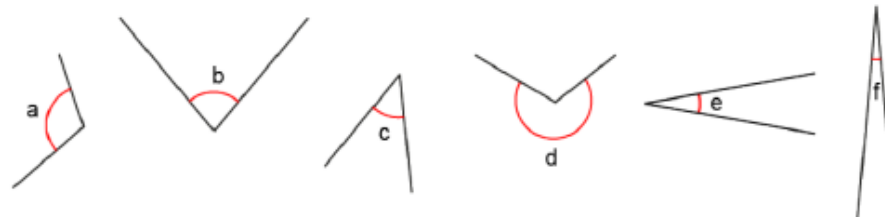
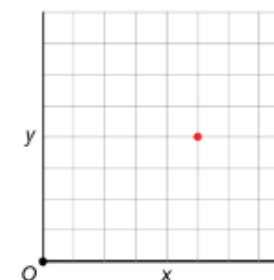
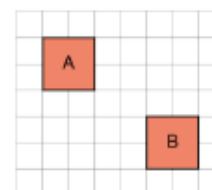
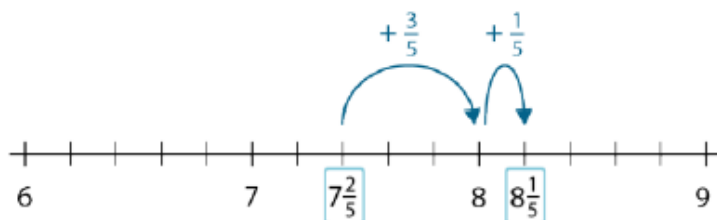
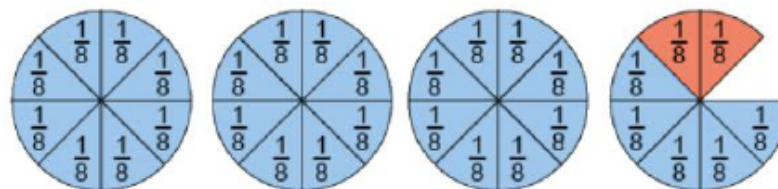
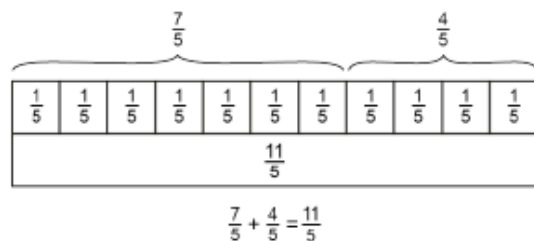
"14 divided into groups of 7 is equal to 2."

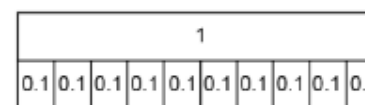
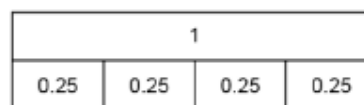
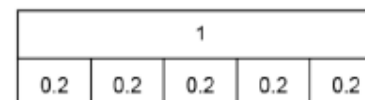
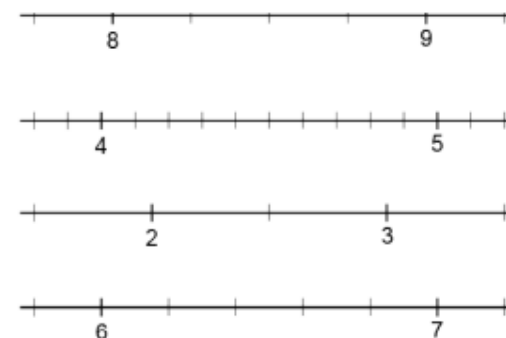
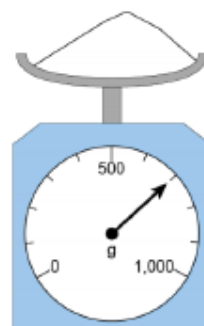
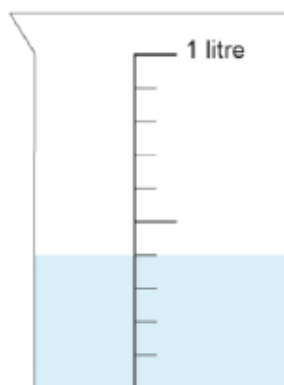
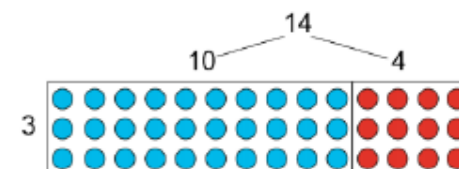
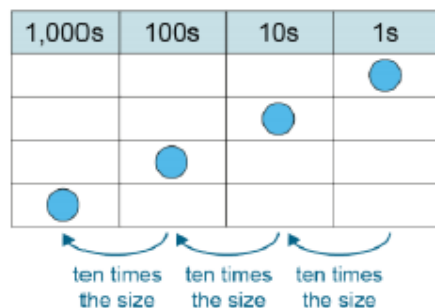
"The 14 represents the total number of eggs."

"The 7 represents the number of eggs in each nest/group."

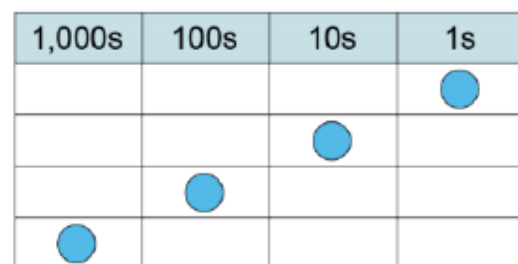
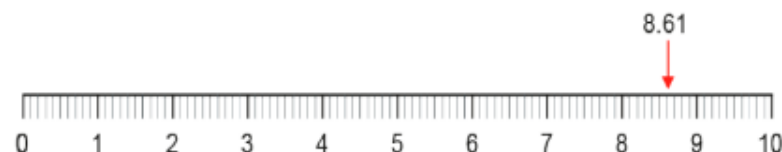
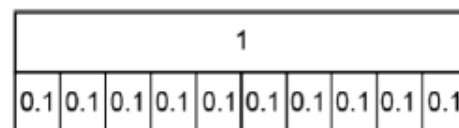
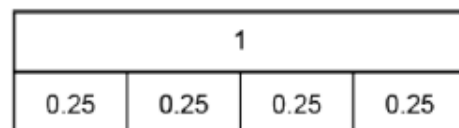
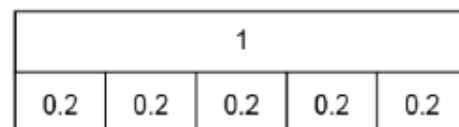
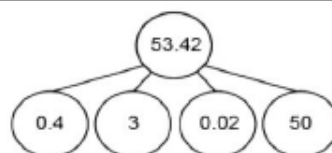
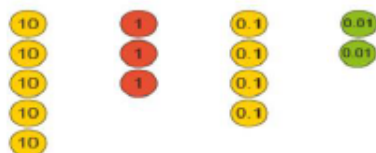
"The 2 represents the number of nests/groups."



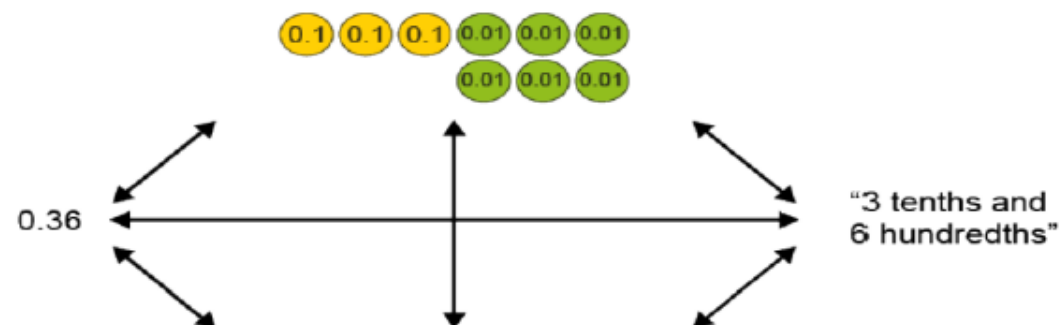




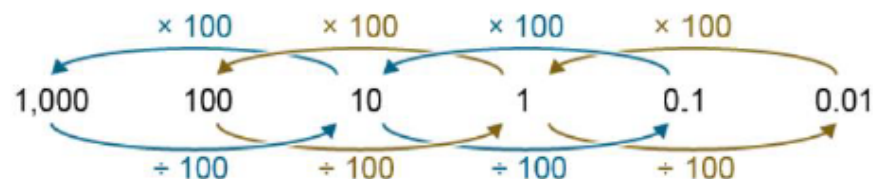
Year 6: 6.1



ten times the size ten times the size ten times the size



1,000	2,000	3,000	4,000	5,000	6,000	7,000	8,000	9,000
100	200	300	400	500	600	700	800	900
10	20	30	40	50	60	70	80	90
1	2	3	4	5	6	7	8	9
0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09



1,000	2,000	3,000	4,000	5,000	6,000	7,000	8,000	9,000
100	200	300	400	500	600	700	800	900
10	20	30	40	50	60	70	80	90
1	2	3	4	5	6	7	8	9
0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09

$8 \div 10 = 0.8$ $0.8 \times 10 = 8$

1,000s	100s	10s	1s	0.1s	0.01s
			8		
			0	8	

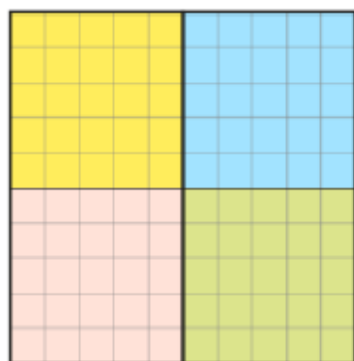
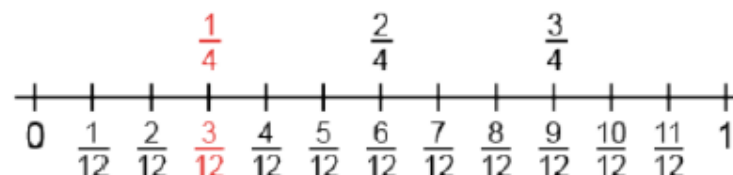
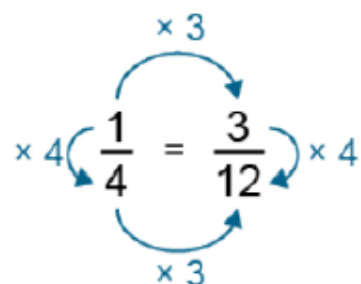
$8 \div 10 = 0.8$ $0.8 \times 10 = 8$

Informal written method	Expanded multiplication algorithm	Short multiplication																														
$34 \times 2 = 30 \times 2 + 4 \times 2$ $= 60 + 8$ $= 68$	<table><tr><td></td><td>10s</td><td>1s</td></tr><tr><td></td><td>3</td><td>4</td></tr><tr><td>x</td><td></td><td>2</td></tr><tr><td></td><td></td><td>8</td></tr><tr><td></td><td>6</td><td>0</td></tr><tr><td></td><td>6</td><td>8</td></tr></table> $2 \times 4 \text{ ones} = 8 \text{ ones}$ $2 \times 3 \text{ tens} = 6 \text{ tens}$		10s	1s		3	4	x		2			8		6	0		6	8	<table><tr><td></td><td>10s</td><td>1s</td></tr><tr><td></td><td>3</td><td>4</td></tr><tr><td>x</td><td></td><td>2</td></tr><tr><td></td><td>6</td><td>8</td></tr></table>		10s	1s		3	4	x		2		6	8
	10s	1s																														
	3	4																														
x		2																														
		8																														
	6	0																														
	6	8																														
	10s	1s																														
	3	4																														
x		2																														
	6	8																														

Short division with place-value counters	Short division
$8 \text{ tens} \div 4 = 2 \text{ tens}$ $4 \text{ ones} \div 4 = 1 \text{ one}$	$8 \text{ tens} \div 4 = 2 \text{ tens}$ $4 \text{ ones} \div 4 = 1 \text{ one}$

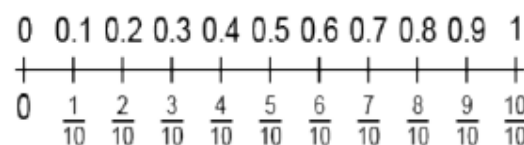
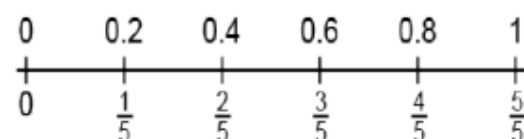
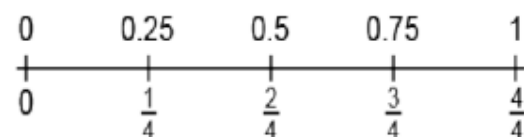
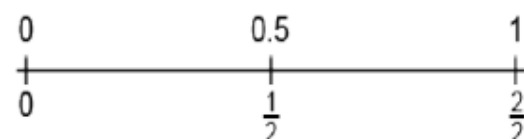
Figure 29: dividing 84 by 4 using short division with place-value counters

Figure 30: dividing 84 by 4 using short division with place-value headings

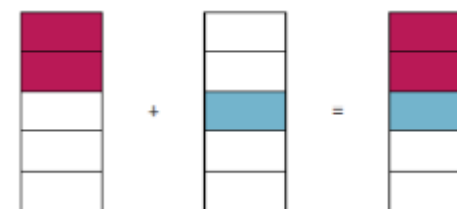


$$\frac{1}{4} = 25\%$$

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As the diagram shows, it is true that $\frac{2}{5} + \frac{1}{5} = \frac{3}{5}$



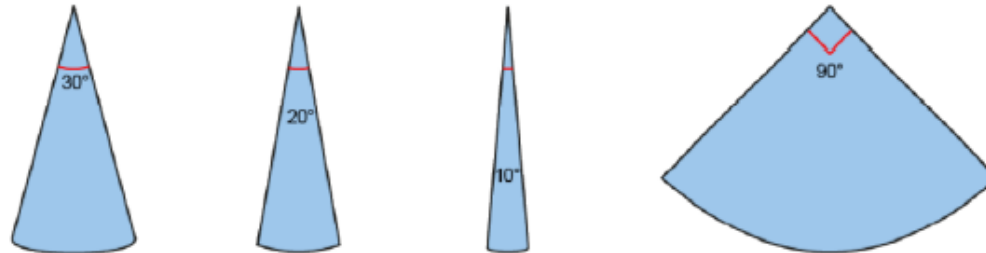
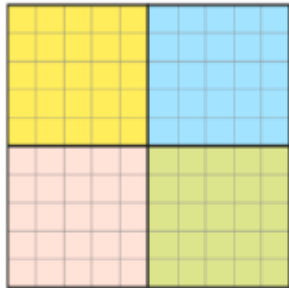
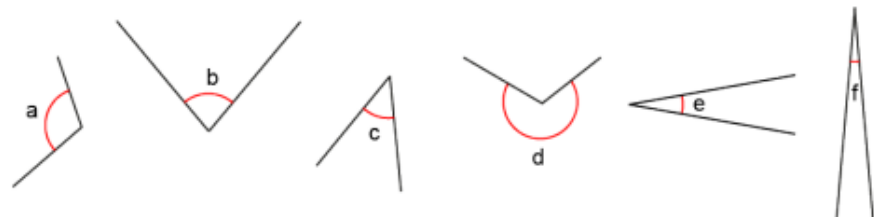


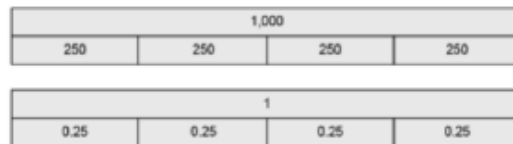
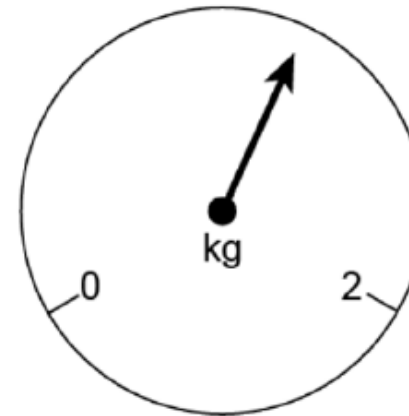
Figure 45: a selection of 'standard angle' measuring tools



1,000	2,000	3,000	4,000	5,000	6,000	7,000	8,000	9,000
100	200	300	400	500	600	700	800	900
10	20	30	40	50	60	70	80	90
1	2	3	4	5	6	7	8	9
0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09

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Distance in km expressed as a fraction	Distance in km expressed as a decimal fraction	Distance in metres
$\frac{1}{5}$ km	0.2km	200m
$\frac{1}{4}$ km	0.25km	250m
$\frac{1}{2}$ km	0.5km	500m
$\frac{3}{4}$ km	0.75m	750m
$\frac{1}{10}$ km	0.1km	100m
all other multiples of $\frac{1}{10}$ km, for example, $\frac{7}{10}$ km	0.7km	700m



$\times 10$

100	200	300	400	500	600	700	800	900
10	20	30	40	50	60	70	80	90
1	2	3	4	5	6	7	8	9
0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09

$8 \div 10 = 0.8$ $0.8 \times 10 = 8$

Figure 25: using the Gattegno chart to multiply and divide by 10, crossin

